# Graduating the Saudi Crude Mortality Rates and Constructing Their Monetary Tables

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Abstract. The actuarial method to develop a law of mortality or a mathematical expression to graduate the Saudi crude mortality rates have been applied, also monetary tables have been constructed to assist calculating the actuarial present value for the Saudi life annuities (SPVA).

#### 1. Introduction

Graduation may be regarded as the principles and methods by which a set of observed (or crude) probabilities are adjusted in order to provide a suitable basis for inferences to be drawn and further practical computations to be made.

The fundamental justification for the graduation of a set of observed probabilities like  $q_x$  is the premise that if the number of individuals in the group on whose experience the data are based,  $n_x$  had been considerably large, the set of observed probabilities would have displayed a much more regular progression with x. In the limit with  $n_x$  indefinitely large, the set of probabilities would thus exhibited a smooth progression with x. Therefore, the observed data may be regarded as a sample from a larger population so that the observed probabilities, derived there from, are subject to sampling errors. Providing these errors are random in nature, they may be reduced by increasing the size of the sample and thereby extending the scope of the investigation. A simpler, cheaper and more practicable alternative is often to use graduation to remove these random errors.

#### 2. Graduation Methods

The actuarial methods of graduation can be described broadly as [1]:

- 2.1. The graphic method consists of drawing a graph through or near the crude values of the function to be smoothed. Smoothness has been alleged to be achieved or improved by hand-polishing the values to make the third differences as small as possible.
- 2.2. The summation method consists of applying a finite difference forms involving successive summations to the crude values. The accepted 'smoothing coefficients' or 'smoothing index' is related to third differences and it follows that the more powerful smoothing index of the formula chosen, the closer it comes to the fitting of polynomial.
- 2.3. The Kernel's method is an elegant variation of the summation methods, which avoids the necessity of filling in the smoothed values at the two ends of the tables [2].
- 2.4 The method of osculatory interpolation, which aims at achieving identical third differences at points where different sections of the smoothed function meet one another.
- 2.5. The spline method is a variation on the method of osculatory interpolation, but third differential coefficients take the place of the third differences.
- 2.6. The curve fitting or parametric method, or the fitting of a formula which produces a suitable shape, it has sometimes been said to give ideally smooth results, but whether it does must surely depend upon which formula or curve has been fitted.
- 2.7. Graduation by reference to a standard table which depends on establishing a relationship between the crude rate and the rate obtained from the standard table by applying them on a simple formula. Clearly the degree of smoothness must depend very largely upon the smoothness of the standard table used.
- 2.8. The difference equation method determines the graduated series by a difference equation derived from an analytic measure of the relative emphasis placed on smoothness and fit.
- 2.9. The linear programming method determines the graduated series by minimizing the divergence index subject to constraints.

Graduation is characterized by two essential qualities, smoothness and fit. An increase in smoothing results a reduction in fit. Conversely, when fit is improved, smoothness usually suffers. The following preliminary test for the Saudi crude mortality rates suggest using the curve fitting method (mathematical model) for graduation.

#### 3. The Preliminary Test for a Mathematical Model

The first important contribution towards finding a mathematical model was made by Benjamin Gompertz (1825), who argued that the force of mortality  $\mu_x$  can be represented by the formula  $BC^x$ .

A development of Gompertz's law was subsequently made by Makeham (1860), who adapted the formula:

$$\mu_{\mathbf{r}} \quad \text{or} \quad q_{\mathbf{r}} = A + BC^{\mathbf{x}} \tag{1}$$

when Gompertz's law holds the graph of the following equation is a straight line [3]:

$$-\ln(-\ln(1-q_x)) = \ln\left(\frac{\ln C}{B(C-1)}\right) - x \ln C$$
 (2)

Also, a Makeham gradution appears justified and estimates of C and B can be obtained by sketching the line and noting it's slope and y-intercept:

$$\hat{C} = \exp(-slope) \tag{3}$$

$$\hat{B} = \frac{\ln \hat{C}}{(\hat{C} - 1)} \exp(-int ercept)$$
 (4)

Graduated rates can be then calculated by the use of an eight-parameter formula [4] for the age curve of mortality:

$$q_x = A^{(x+B)^C} + D \exp\left(-E\left(\ln\frac{x}{F}\right)^2\right) + \frac{GH^x}{1 + GH^x}$$
 (5)

where  $q_x$  is the probability of someone exact age x dying before exact age x+1, and A, B,..., H are parameters to be estimated. The parameters are estimated by least squares criteria, minimizing the sum of squares of the proportional differences of the fitted from the observed mortality probabilities, after regrouping into age groups. The least squares fitting criterion produce a smoothed set of  ${}_5q_x$  values and single-year  $q_x$  values which aggregate to the smoothed  ${}_5q_x$  values. The fit is usually very good and this procedure appears to provide excellent fits for the additional life table columns also [5].

The mathematical formula in Eq. (5) contains three terms each representing a distinct component of mortality [4]:

The first term representing a rapidly declining exponentially, reflects the fall in mortality during the early childhood years as the child adapts to his or her new environment and gains immunity from the diseases of the outside world, this term has three parameters:

- A: which is nearly equal to  $q_i$ .
- B: is an age displacement, it measures the location of infant mortality.
- C: measures the rate of mortality decline in childhood, the higher the value of C, the faster mortality declines with increasing age.
- The second term is a function similar to the lognormal, reflects accident mortality for males and accident plus maternal mortality for the female population. It has three parameters:
  - D: measuring the severity.
  - E: representing spread.
  - F: indicating location.
- The third term in the formula, the well-known Gompertz exponential, reflects the near geometric rise in mortality and it is generally considered the aging of the body, i.e. senescent mortality, and it has two parameters:
  - G: represents the base level of senescent mortality.
  - H: represent the rate of increase of that mortality.

The mortality rates of insured Saudi persons were assumed equal to those of the general population. Mortality rates of invalidity pensioners and survivors were assumed equal to the mortality of active insured persons. Crude rates appear in Table 1 [6]:

Table 1. Saudi crude mortality rates

Age interval	$q_x^0$ Male	$q_x^{\circ}$ Female
10 -	0.00209	0.00126
15 -	0.00292	0.00175
20 -	0.00408	0.00243
25 -	0.00569	0.00337
30 -	0.00794	0.00468
35 -	0.01106	0.00651
40 -	0.01541	0.00904
45 -	0.02151	0.01255
50 -	0.02998	0.01744
55 -	0.04183	0.02423
60 -	0.05834	0.03365
65 -	0.08136	0.04675
70 -	0.11463	0.06494
75 -	0.15825	0.09021
80 -	0.22068	0.12531
85 -	0.30778	0.17407
90 -	0.42926	0.24180

Applying the preliminary test on the above data, it suggests a straight line in each case for male (Fig. 1) and female (Fig. 2).

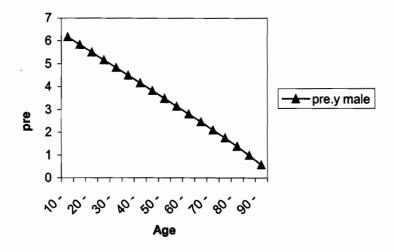


Fig. 1. Preliminary tests (male).

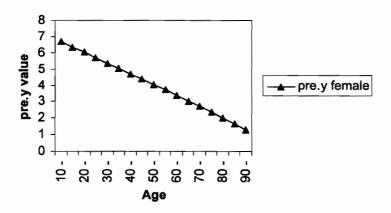


Fig. 2. Preliminary tests (female).

Both figures suggesting fitting a mathematical formula to graduate and represent the Saudi rates.

#### 4. Fitting the Model

Various curve fitting have been tried [7, 8], which failed to represent the Saudi data. Heligman and Pollard mathematical formula Eq. (5) could represent the Saudi rates. The central mortality rates were transformed to  $q_x$  values by the classical formula:

$$q_X^0 = \frac{2m_X}{2 + m_Y} \tag{6}$$

The parameters of the curve were estimated by least squares Gauss-Newton iteration [9]. The function minimized was:

$$S^{2} = \sum_{x=0}^{85} \left( \frac{q_{x}}{q_{x}^{0}} - 1.0 \right)^{2} \tag{7}$$

where  $q_x$  is fitted value at age x and  $q_x^0$  is the observed (crude) mortality rate. That is, the sum of the squares of the proportional difference between the fitted and observed rates was minimized. The observed rates above age 85 will be excluded from the calculation because they appeared to be less reliable. Using the procedure UNABR from the United Nations Software Package for Mortality Measurement (MortPak-Lite), the graduated life tables for both sex are presented in Appendix I, also their parameters are presented in Table 2.

Table 2. Graduation parameters for Saudi mortality experience 1990-1993

Parameter	Males	Females
Α	0.02779	0.01776
В	0.56113	0.82686
C	0.43809	0.37970
D	0.00119	0.00012
E	0.86895	1.83524
F	63.37608	23.35901
G	0.00012	0.00007
Н	1.08145	1.08175

Comparing between the Saudi parameters of males and females in Table 2, males have experienced higher child mortality than females (156.48%), which appears from the values of parameter A. Also, the higher B value for females indicate that they have relatively lower infant mortality, in the same time males have higher value of C, i.e. their rate of mortality decline with age has been faster. Parameter D for male is higher than the female, may be that return to some accident mortality, and the following figure (Fig. 3) representing Saudi pattern of mortality for both genders.

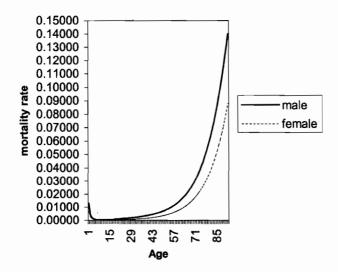


Fig. 3. Saudi pattern of mortality.

#### 5. Monetary Saudi Tables

Commutation functions are derived by combining life table functions with compound interest functions, to construct the monetary tables based on the Saudi mortality rates obtained over the available range of ages. Life tables can be built up by starting with any suitable radix, say 100000, and applying successfully the relations [10]:

$$d_x = l_x q_x \tag{8}$$

$$l_{x+1} = l_x - d_x \tag{9}$$

where  $l_x$  indicating the survivors to the exact age x, and  $d_x$  indicating the number of deaths between x and x+1. Also, a computer program has been written in VISUAL BASIC.NET to compute the commutation functions in Eqs. (10) and (11) for ages

starting from 10 to 99 inclusively for both Saudi males and females, and interest rate  $\nu = 5\%$  (as an example). The monetary tables have been represented in (Appendix II):

$$D_{x} = v^{x} \cdot l_{x}$$

$$N_{x} = \sum_{t=0}^{\infty} D_{x+t}$$

$$S_{x} = \sum_{t=0}^{\infty} N_{x+t}$$

$$(10)$$

$$C_{x} = v^{x+1} \cdot d_{x}$$

$$M_{x} = \sum_{t=0}^{\infty} C_{x+t}$$

$$R_{x} = \sum_{t=0}^{\infty} M_{x+t}$$
(11)

There are also other commutation functions used for the techniques of valuation of pension benefits that the researchers will deal with them in another article. To show some comparisons between Saudi life annuities for male and female, we use the calculated tables (Appendix II) and the following equation:

$$\ddot{a}_x = \frac{N_x}{D_x} \tag{12}$$

where,  $\ddot{a}_x$ : a life annuity-due which is a series of payments of one unit at the beginning of each year, payable as long as a life aged x is alive, and it can be expressed in terms of the elementary commutation functions as indicated. If the payments are made at the end of each year, the annuity is termed an immediate life annuity. It is denoted by the symbol  $a_x$  and has the following expression:

$$a_x = \frac{N_{x+1}}{D_x} \tag{13}$$

Some comparisons are made to distinguish between the annuities of both sexes at different ages when the interest rate equal 5% in Table 3 and Table 4:

Table 3	The probable	present value	of a Saudi lif	e annuity_due
i abie 5.	THE DIODADIE	Dresent value	OLA SAUGI III	e ammuntv-uue

Age (x)	$\ddot{a}_x$ Male (1)	$\ddot{a}_x$ Female (2)	Ratio (2/1)%
30	17.95	18.86	103.07
40	16.61	17.77	106.98
50	14.81	16.24	109.66
60	12.56	14.20	113.06

Table 4. The probable present value of a Saudi immediate life annuity-due

Age (x)	<i>a<sub>x</sub></i> Male (1)	a <sub>x</sub> Female (2)	Ratio (2/1)%
30	16.95	17.86	105.37
40	15.61	16.77	107.43
50	13.31	15.24	110.35
60	11.56	13.20	114.19

It is clear from Tables 3 and 4 that both life annuities are higher for females, which will represent higher premium for them. This is acceptable if we consider their lighter mortality rates, which will give the females few years to maturity.

#### 6. Conclusion

This article is adopting a law of mortality suggested by Heligman and Pollard [4] to graduate the Saudi crude rates. Its mathematical formula contains three terms, each representing a distinct component of mortality. The curve is continuous and applicable over the entire age range. It has relatively few parameters all of which have demographic interpretation and together fully describe the Saudi age pattern of mortality for males and females. Also, monetary tables have been constructed by using a computer program written in VISUAL BASIC.NET to assist calculating the actuarial present values for the Saudi life annuities (SPVA). Some comparisons are made to distinguish between the annuities of both sexes at different ages.

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## Appendix I

## Saudi Life Table (Females)

AGE	M(X,N)	Q(X,N)	I(X)	E(X)	AGE	M(X,N)	Q(X,N)	I(X)	E(X)
0	.06486	.06205	100000	68.27	52	.00840	.00836	81712	26.65
1	.01306	.01297	93795	71.76	53	.00899	.00895	81028	25.87
2	.00463	.00462	92578	71.70	54	.00964	.00959	80303	25.10
3	.00209	.00209	92151	71.03	55	.01033	.01028	79532	24.33
4	.00111	.00111	91959	70.18	56	.01108	.01102	78715	23.58
5	.00069	.00069	91856	69.25	57	.01188	.01181	77848	22.84
6	.00049	.00049	91793	68.30	58	.01275	.01267	76929	22.11
7	.00040	.00040	91748	67.34	59	.01369	.01360	75954	21.38
8	.00036	.00036	91711	66.36	60	.01471	.01460	74921	20.67
9	.00036	.00036	91678	65.39	61	.01580	.01568	73827	19.97
10	.00038	.00038	91645	64.41	62	.01698	.01684	72670	19.28
11	.00040	.00040	91610	63.43	63	.01826	.01809	71446	18.60
12	.00044	.00044	91573	62.46	64	.01964	.01944	70153	17.93
13	.00049	.00049	91533	61.49	65	.02112	.02090	68789	17.28
14	.00054	.00054	91488	60.52	66	.02273	.02247	67351	16.64
15	.00060	.00060	91438	59.55	67	.02446	.02416	65838	16.01
16	.00067	.00067	91383	58.58	68	.02633	.02599	64247	15.39
17	.00074	.00074	91322	57.62	69	.02835	.02795	62577	14.79
18	.00081	.00081	91255	56.67	70	.03053	.03007	60828	14.20
19	.00089	.00089	91181	55.71	71	.03287	.03234	58999	13.63
20	.00097	.00097	91100	54.76	72	.03541	.03479	57091	13.07
21	.00105	.00105	91012	53.81	73	.03814	.03743	55104	12.52
22	.00114	.00114	90916	52.87	74	.04109	.04026	53042	11.99
23	.00124	.00124	90812	51.93	75	.04427	.04331	50906	11.47
24	.00134	.00134	90699	50.99	76	.04769	.04658	48702	10.96
25	.00144	.00144	90578	50.06	77	.05138	.05009	46433	10.48
26	.00155	.00155	90448	49.13	78	.05536	.05386	44107	10.00
27	.00166	.00166	90308	48.21	79	.05964	.05791	41731	9.54
28	.00178	.00177	90159	47.29	80	.06424	.06224	39315	9.10
29	.00190	.00190	89999	46.37	81	.06920	.06689	36868	8.67
30	.00203	.00203	89828	45.46	82	.07454	.07186	34402	8.25
31	.00217	.00216	89646	44.55	83	.08027	.07718	31929	7.85
32	.00231	.00231	89452	43.64	84	.08644	.08286	29465	7.47
33	.00246	.00246	89245	42.74	85	.09306	.08893	27024	7.10
34	.00262	.00262	89025	41.85	86	.10018	.09540	24620	6.74
35	.00280	.00279	88792	40.96	87	.10781	.10230	22272	6.40
36	.00298	.00297	88544	40.07	88	.11600	.10964	19993	6.07
37	.00317	.00317	88281	39.19	89	.12477	.11744	17801	5.76
38	.00338	.00337	88002	38.31	90	.13417	.12573	15711	5.46
39	.00359	.00359	87705	37.44	91	.14422	.13452	13735	5.17
40	.00383	.00382	87390	36.57	92	.15498	.14383	11887	4.90
41	.00408	.00407	87056	35.71					
42	.00435	.00434	86702	34.85					
43	.00463	.00462	86326	34.00					
44	.00494	.00493	85927	33.16	PAI	RAMETERS:	A= .027	79 B=	.56113
45	.00527	.00526	85503	32.32			C= .438		.00119
46	.00563	.00561	85054	31.49			E= .868		3.37608
47	.00601	.00599	84577	30.66			G= .000		1.08145
48	.00642	.00640	84070	29.84					
49	.00686	.00684	83532	29.03					
49 50	.00686	.00684	83532 82961	29.03 28.23					

## Saudi Life Table (Males)

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AGE	M(X,N)	Q(X,N)	I(X)	E(X)	AGE	M(X,N)	Q(X,N)	I(X)	E(X)
0	.06486	.06205	100000	68.27	52	.00840	.00836	81712	26.65
1	.01306	.01297	93795	71.76	53	.00899	.00895	81028	25.87
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15	.00060	.00060	91438	59.55	67	.02446	.02416	65838	16.01
16	.00067	.00067	91383	58.58	68	.02633	.02599	64247	15.39
17	.00074	.00074	91322	57.62	69	.02835	.02795	62577	14.79
18	.00081	.00081	91255	56.67	70	.03053	.03007	60828	14.20
19	.00089	.00089	91181	55.71	71	.03287	.03234	58999	13.63
20	.00097	.00097	91100	54.76	72	.03541	.03479	57091	13.07
21 22	.00105	.00105	91012 90916	53.81 52.87	73 74	.03814	.03743	55104 53042	12.52 11.99
23	.00114	.00114	90916	51.93	75	.04109	.04331	50906	11.47
24	.00124	.00124	90699	50.99	76	.04769	.04658	48702	10.96
25	.00134	.00134	90578	50.06	77	.05138	.05009	46433	10.48
26	.00155	.00155	90448	49.13	78	.05536	.05386	44107	10.00
27	.00166	.00166	90308	48.21	79	.05964	.05791	41731	9.54
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38	.00338	.00337	88002	38.31	90	.13417	.12573	15711	5.46
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43	.00463	.00462	86326	34.00			• 005	170 5	5 61 1 2
44	.00494	.00493		33.16	PA	RAMETERS:			.56113
45	.00527	.00526	85503	32.32			C= .438		.00119
46	.00563	.00561	85054	31.49			E= .868		3.37608
47	.00601	.00599	84577	30.66			G = .000	)12 H=	1.08145
48	.00642	.00640	84070	29.84 29.03					
49 50	.00686	.00684	83532 82961	29.03					
51	.00785	.00731	82355	27.43					
J 1	.00/03	.00762	02333	27.43					

# Appendix II

### Saudi Monetary Table (Interest rate 5% and Males)

Age(x)	Dx	Nx	Sx		Age(x)	Cx	Mx	Rx	
1	0 61391	1206456	21559879		10	22	3919	177832	
1	1 58446	1145065	20353423		11	22	3898	173913	ì
1		1086619	19208358		12	23	3876	170015	
1			18121739	18	13	24	3853	166139	-
1		978008	17090762		14	25	3829	162286	и
1	5 47996	CONTRACTOR OF THE PARTY OF THE	16112753		15	27	3803	158457	и
1	the contract of the contract o	879590	15185167	ш	16	28	3776	154654	
1		833907	14305578		17	30	3748	150878	1
1		790427	13471671		18	31	3718	147130	н
1	THE RESERVE TO SHOULD AND THE PERSON.	749048	12681244		19	33	3687	143412	
2		709670	11932196		20	34	3654	139725	
2		672201	11222526	-	21	35	3620	136071	
2			10550325		22	36	3585	132451	п
2		602630	9913776		23	37	3549	128866	-
2	THE RESERVE OF THE PARTY OF THE	570363	9311146		24	38	3512	125317	
2	PERSONAL PROPERTY AND ADDRESS OF THE PARTY AND	539669	8740783		25	39	3473	121805	
2		510476	8201113		26	40	3434	118332	и
2		482711	7690637		27	41	3394	114898	
2	The second secon	456309	7207926	-	28	42	3353	111504	
2		431205	6751617	12	29	42	3312	108151	
3		407338	6320411	100	30	43	3269	104839	
3		384650	5913073		31	44	3226	101570	
3		363085	5528423		32	44	3183	98343	8
3	The second secon	342591	5165338	-	33	45	3139	95161	
3			4822747	18	34	45	3094	92022	и
	5 17576		4499630		35	46	3049	88929	п
3			4195015		36	.46	3003	85/880	и
3		5-W 1941	3907976		37	47	2957	82877	и
	8 15051	254494	3637631		38	47	2910	79920	
3		239443	3383137		39	48	2863	77010	
4	Commence of the Commence of th	225156	3143694		40	48	281/5	74148	а
4			2918538		41	49	2767	71333	
4	The second contract of		2706940		42	49	2718	1685861	100
4		186530	2508207		43	50	2669	65848	
4	STREET, SQUARE, SQUARE	174957	2321677		44	50	261.9	63173	-
4		163964	2146721		45	51	2569	60559	
4		153585	1982737		46	51	2518	57990	-
4	The second secon	143731	1829152		47	52	2467	55472	-
4		1343198	1685421		48	52	2415	53005	1
4		125561	1551023		49	53	2363	50590	
5	The second secon		1425463		50	54	2310	48227	-
5	Contraction of the Contraction	109285	1308265		51	54	2256	45227	-
5		101803	1198980		52	55	2202	43662	-
5			1097177		53	55	2147	41460	
5			1.002445		54	56	2091	39313	
5			914393		55	5.7	2035	37222	-
5			914393 832647	-	56	157	1979	3722:2	1

## Saudi Monetary Table (Interest rate 5% and Males)

Monetary Tables for Males									
e(x)	Dx	N×	Sx		Age(x)	Cx	Mx	Rx	
55		81746		188	55	57	2035	37222	
56	THE RESERVE THE PERSON NAMED IN COLUMN TWO IS NOT THE PERSON NAMED IN COLUMN TWO IS NAMED IN COLUMN TWO I	-	AND DESCRIPTION OF THE PERSON NAMED IN		56	57	1979	35186	
57		70186	756851		57	58	1922	33207	
58		-	686665		58	58	1864	31286	
59	the second secon	59924	621765		59	59	1806	29422	
60	The second second second	55243	561841		60	59	1747	27616	
61		50844	506597		61	60	1687	25870	
62	The second secon	46714	455753		62	60		24182	
63	Commence of the Commence of th	42841	409039		63	61	1567	22555	
64	CONTRACTOR OF THE PARTY OF THE	39212	366198		64	61	1506	20988	
65	-	35817	326987		65	61	1445	19482	
66			291170	100	66	62	1384	18037	
67	The second second second	taken and	258526	100	67	62		16653	
68		26926	228842	100	68	62		15331	
69		24362	201915	100	69	62	1199	14070	
70	The second second second second		177554	100	70	61	1137	12872	
71	Contract of the Contract of th	THE RESERVE THE PERSON NAMED IN	155573		71	61	1076	11734	
72		17735	135798		72	61	1015	10658	
73		15854	118062	-	73	60	955	9643	
74			102208		74	59		8688	
75		12534	86086		75	58	-	7794	
78		11079	75552		76	57	777	6958	
77			64473		77	56	720	6181	
78			54720		78	54	664	5460	
79		7453			79	53		4796	
80	THE RESERVE OF THE PERSON NAMED IN	6467	38721		80	51	557	4186	
81					81	49	506	3629	
82			-		82	47	457	3123	
83	626	4080	21888		83	45	410	2666	
84	551	3454	17809		84	42	365	2257	
85	483	2902	14355		85	40	323	1891	
86	420	2419	11453		86	37	283	1568	
87	7 363	1999	9034	100	87	34	246	1285	
88	311	1636	7034		88	32	212	1039	
89	265	1325	5398		89	29	180	828	
90	223	1060	4074	18	90	26	151	648	
91	187	836	3014	18	91	23	125	496	
92		649	2178	100	92	21	102	371	
93		495	1528		93	18	81	269	
94	103	368	1033		94	16	63	188	
95		266	665		95	13	48	125	
96	65	184	400		96	11	34	77	
97		119	THE RESERVE OF THE PARTY OF THE		97	9		43	
96		-			98	8	14	20	
99					99	6		6	

## Saudi Monetary Table (Interest rate 5% and Females)

	Monetary Tables for Females										
Age(x)	Dx		Nx	Sx		Age(x)	Cx	Mx		Rx	-
1	0	61391	1233399	22917821		10	1	3	2567	133921	ı
1	1	58454	1172008	21684422		11	1	3	2554	131353	ı
	2	55658	1113553	20512414		12	1	4	2541	128799	1
1	3	52993	1057896	19398861		13	1	4	2527	126259	1
	4	50456	1004902	18340966	-	14	1	4	2513	123732	1
	5	48039	954446	17336063	-	15	1	5	2498	121219	1
	6	45736	906408	16381617		16	1	5	2484	118721	1
	7	43543	860671	15475209	-	17	1	5	2468	116237	1
1	8	41454	817128	14614538		18	1		2453	113769	١
	9	39465	775674	13797410	-	19	1	-	2437	111316	1
2	0	37569	736209	13021736	-	20	1		2421	108879	1
	1	35764	698640	12285527		21	1	_	2405	106458	
	2	34045	662875	11586887		22	1	_	2389	104053	
	3	32407	628830	10924012		23	1	THE RESIDENCE AND ADDRESS.	2372	101664	
	4	30847	596423	10295182	-	24	1		2355	99292	1
	5	29361	565577	9698758	-	25	1		2338	96937	١
	6	27945	536216	9133182		26	1	-	2321	94599	1
	7	26597	508271	8596966		27	1		2303	92278	١
	8	25313	481674	8088695	100	28	1		2285	89975	١
	9	24089	456361	7607022		29		-	-		١
	0	22924	432272	7150661		30	1		2267	87690	١
	1	21814	409348	6718389		Name and Address of the Owner, when the Owner, which the O	and the same of th	_	2249	85422	١
	2	20756	387534	6309042		31	1		2230	83173	١
	3	19749	366777	5921508		33	1		2193	80943 78731	١
	4	18789	347028	5554731					-		١
	5	17875	328239	5207702	18	34	2	-	2173	76538	١
	6	17003	310365	4879463		35	2		2154	74365	1
	7	16173	293361	1040	100	36		-	2133	72211	
				4569099 4275738	100	37	2	_	2113	70078	1
	181	15382	277188		. 100	38	2	-	20192	67965	١
	0	14628	251806	3998549	100	39	2		2070	65873	1
	-	13910	247178	3736743	18	40	2		2049	63903	١
	1	13225	233269	3489565		41	2	-	2026	61754	
	2	12572	220044	3256296	100	42	2	_	2003	59728	
	3	11950	207472	3036252		43	2	-	1980	57725	
	4	11357	195522	2826780		44	CONTRACTOR CONTRACTOR CONTRACTOR	5	1956	55745	
	5	10791	184165	2633259		45	2		1931	53789	
	6	10252	173374	2449093		46	2	_	1906	51858	
	7	9738	1631/21	2275720		47	2		1880	49952	
	8	9248	153383	2112598		48	2	_	1854	4807.2	
	9	8781	144135	1959215		49	2	_	1826	4621:9	
	0	8335	135354	1815080		50	2		1799	4439/2	
	1	7909	127020	1679726		51	2	_	1770	42594	
	2	7503	119110	1552706		52	3	0	1741	40824	
	3	7116	111607	1433595		53	3	1	1711	3908:3	
5	4	6747	104491	1321988		54	3	1	1680	37372	
	5	5394	97744	1217498		55	3	2	1649	35691	
	E.	6957	91350	1119754	<b>W</b>	56	2	3	1617	34042	

## Saudi Monetary Table (Interest rate 5% and Females)

			Mone	etar	y Tables	for Fen	nales	
Age(x)	Dx	Nx	Sx		Age(x)	Сх	Mx	Rx
5					55	32		35691
5		_			56	33	1617	34042
5			The second second second		57	34	1584	32425
5					58	34	1550	30841
5			863555		59	35		29291
6		And in contrast of the last of	-		60	36	1481	27775
6			720438		61	37	1445	26294
6.			656304		62	37	1408	24849
6			THE RESERVE OF THE PERSON NAMED IN		63	38	1371	23441
6		51120	541549		64	39	1332	22071
6			490429		65	40	1294	20738
6			443167	100	66	40	1254	19445
6			NAME AND ADDRESS OF THE OWNER, WHEN PERSON NAMED IN	100	67	41	1214	18191
6			359333		68	42	1173	16977
6			322346		69	42	1131	15805
7		31124	288383		70	43	1089	14674
7			257259		71	43	1046	13585
7.			228796	-	72	44	1003	12539
7.			202825		73	44	959	11536
7.			179184		74	44	915	10577
7	The second second second second	19438	157719	100	75	45	871	9662
7			138282		76	45	826	8792
7		15798	120731		77	45	782	7965
7			104933	-	78	45	737	7184
7			90759		79	44	692	6447
8		and the second second second second	-		80	44	648	5754
8	1 1171	10009	66804		81	44	604	5106
8	2 1072	8838	56795		82	43	560	4502
8	3 978	7766	47957		83	42	517	3942
8	4 889	6788	40191		84	41	475	3425
8	5 805	5899	33403	100	85	40	434	2950
8	6 726	5094	27504		86	39	393	2516
8	7 652	4368	22410		87	38	354	2123
8			18042		88	37	316	1769
8		3132	14327	100	89	35	279	1454
9	the state of the s	2613	11194		90	33	244	1174
9	-	2154	8581		91	32	211	930
9	2 353	1750	6427		92	30	179	719
9		1397	4676		93	28	150	540
9		1090	3279		94	26	122	391
9			2189		95	23	96	269
9		599	1363		96	21	73	172
9	7 162	407	764		97	19	52	99
9		246	357		98	17	32	48
9	9 111	111	111		99	15	15	15

## تدريج معدلات الوفاة السعودية الخام وبناء حداول رموزها الحسابية

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(قدم للنشر في ١٤٢٦/٢/٢٣هـ؛ وقبل للنشر في ١٤٢٧/١/٢٨هـ)

ملخص البحث. تم في هذا البحث تطبيق الطرق الإكتوارية لإيجاد قانون للوفاة أو تعبير رياضي يمثله وباستخدامه تم ته نديب وتدريج معدلات الوفاة الخام لكل من الذكور والإناث السعوديين، كذلك تم استخدام هذه الاحتمالات المهذبة ومعدل استثمار مركب (٥٪ - كمثال) لبناء جداول الرموز الحسابية اللازمة لتقدير القيم الحالية الإكتوارية لدفعات الحياة السعودية.